# A regression-based estimate of the November 2020 sardine recruitment strength based on the June 2021 recruitment survey result 

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#### Abstract

Summary The regression method developed in 2020 to predict the November 2019 sardine recruitment strength from the estimate from the 2020 recruitment survey is shown to have performed very well (given that the assessment-based estimate of that recruitment is now available). Applying the same method to the result from the 2021 recruitment survey predicts a low November 2020 sardine recruitment compared to 2019, with a $90 \%$ probability of being between $8-40 \%$ of the November 2019 level.


Key words: Sardine, recruitment, regression, survey, assessment

## Introduction

For the sardine population, the November recruitment in year $y-1$ is sampled by the recruitment survey in year $y$. The nature of the stock assessment is such that the recruitment survey result in year $y$ is available prior to the assessment update which provides an estimate for the November recruitment in year $y-1$. By assuming that the historical recruitment survey results are directly proportional to the assessment estimate of recruitment for November of the previous year, an attempt can be made to predict the November recruitment of year $y-1$ based on the survey result of year $y$. The assumed relationship is:

$$
\begin{equation*}
\ln \operatorname{surv}(y)=\ln R(y)+\ln k+e p s(y) \quad e p s(y) \sim N(0, \operatorname{sig} 2) \tag{1}
\end{equation*}
$$

where $R(y)$ is the historical assessment estimate of November recruitment in calendar year $y-1$ and $\operatorname{surv}(y)$ is the corresponding recruitment survey result for historical year $y$. Note that for this document, years shown in the plots correspond to the year of the recruitment survey.

A similar but more complicated exercise was undertaken last year (Butterworth and Ross-Gillespie 2020). Since then, the assessment November recruitment series has been updated (de Moor 2021). Accordingly, two main analyses are conducted here:
(I) Regress the updated November recruitment series (values up to Nov 2018) against the survey series (values up to autumn 2019) to see what the prediction for the November 2019 recruitment estimate would have been, and how that compares to the actual November 2019 estimate from the assessment update.
(II) Regress the entire updated November recruitment series (values up to Nov 2019) against the entire survey series (values up to autumn 2020) to predict what the estimate for the November 2020 recruitment will be, together with the associated uncertainty.

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## Results

Results are shown for three regression options: (a) the entire series, (b) values from 2005 onwards only and (c) the 2005 onwards but with the 2010 point excluded. The analyses were run for (b) and (c) to be consistent with approach taken last year. A plot of $\operatorname{surv}(y)$ against $R(y)$ is shown for the three options in Figure 1, along with the fit from equation (1). A plot of the residuals eps(y) against year from the regression fit is shown in Figure 2 for all options, where $\operatorname{eps}(y)=\ln \operatorname{surv}(y)-\ln \operatorname{sur} v_{-} h a t(y)$. The estimate of $\operatorname{sig}$ for option (a) is 0.45 , for option (b) 0.48 and for option (c) 0.49 .

Table 1 lists the data used in the analyses. Figure 3 provides further diagnostic plots for the fits of equation (1) to the data for option (a) and (b). Figure 4 plots log-normal distributions for analyses (I) and (II) where the median of the distribution is (I) the expected 2019 November recruitment estimate that would have been predicted last year using the current assessment recruitment series (plotted alongside the actual 2019 estimate that is now available) and (II) the expected 2020 November recruitment estimate based on the 2021 survey result. The CVs of the normal distributions are given by the standard deviation of the epsilon values of the regression analysis. Figure 5 plots of the November recruitment estimates against year to compare with the point estimates from the regressions.

## Discussion

It is immediately evident from the top panel of Figure 4 that all three regressions from 2020 provided very good estimates of the final November 2019 recruitment of 42.7 as determined from the subsequent assessment (which made use also of the November 2020 survey result).

Repeating this estimation process one year later using the 2021 sardine recruitment survey estimate provides November 2020 sardine recruitment estimates ranging from 7.0 to 8.3, with a lower 5th\%ile from 3.19 to 3.98 and upper 95 th\% from 15.21 to 17.24.

Very clearly, this approach indicates a November 2020 sardine recruitment to be much less than that the year before - at a fraction between 0.08 and 0.40 thereof. The point estimates are close to the second lowest historical value.

## References

Butterworth, D.S, and Ross-Gillespie, A. 2020. Continuous approach applied to sardine recruitment survey estimate to advise on juvenile sardine TAB estimates for 2020 and the corresponding recruitment strength. DEFF Fisheries document FISHERIES/2020/JUL/SWG-PEL/60.
de Moor, C.L. 2021. Updated assessment of the South African sardine resource using data from 1984-2020. DEFF Fisheries document FISHERIES/2021/APR/SWG-PEL/23.

Table 1: Data used in the analyses. The assessment estimates for November recruitment (in billions of fish) in year $y-1$ are linked to (and regressed against) the recruitment survey estimate in year $y$, which is why two year columns are listed. The regression for option (a) uses the data for all years to 2020, option (b) excludes data prior to 2005 and option (c) further excludes the year 2010. Note that throughout this document, where references are made to years such as in the preceding sentence, these values correspond to the year of the recruitment survey estimate. The assessment estimates of November recruitment were provided by C.L de Moor (as per analyses of de Moor 2021), and the recruitment survey estimates provided by J. Coetzee (pers. comm.). Note that the 2020 recruitment survey estimate of 11.777 was updated after Butterworth and Ross-Gillespie (2020) was tabled, and hence differs from the value of 7.01 used in that document.

| Assessment Year | Assessment estimate of November recruitment | Survey Year | Recruitment survey estimate |
| :---: | :---: | :---: | :---: |
| 1984 | 10.3816 | 1985 | 3.592 |
| 1985 | 15.3525 | 1986 | 3.691 |
| 1986 | 20.1740 | 1987 | 7.380 |
| 1987 | 5.4273 | 1988 | 0.440 |
| 1988 | 13.9012 | 1989 | 2.137 |
| 1989 | 16.1823 | 1990 | 2.502 |
| 1990 | 11.0028 | 1991 | 1.915 |
| 1991 | 25.8954 | 1992 | 5.633 |
| 1992 | 64.1250 | 1993 | 15.238 |
| 1993 | 9.0961 | 1994 | 2.654 |
| 1994 | 60.2353 | 1995 | 25.388 |
| 1995 | 13.3146 | 1996 | 3.204 |
| 1996 | 113.0330 | 1997 | 36.856 |
| 1997 | 61.3317 | 1998 | 10.716 |
| 1998 | 65.4672 | 1999 | 10.378 |
| 1999 | 81.3913 | 2000 | 20.002 |
| 2000 | 205.8350 | 2001 | 60.065 |
| 2001 | 173.7780 | 2002 | 49.153 |
| 2002 | 147.8270 | 2003 | 36.448 |
| 2003 | 22.3562 | 2004 | 4.089 |
| 2004 | 12.5670 | 2005 | 2.858 |
| 2005 | 21.6173 | 2006 | 9.506 |
| 2006 | 11.0874 | 2007 | 2.995 |
| 2007 | 18.0642 | 2008 | 4.090 |
| 2008 | 20.2347 | 2009 | 9.289 |
| 2009 | 84.3697 | 2010 | 35.569 |
| 2010 | 16.2999 | 2011 | 5.799 |
| 2011 | 25.4825 | 2012 | 7.986 |
| 2012 | 27.7333 | 2013 | 12.586 |
| 2013 | 8.9938 | 2014 | 1.985 |
| 2014 | 10.4432 | 2015 | 6.258 |
| 2015 | 6.7885 | 2016 | 0.811 |
| 2016 | 12.8972 | 2017 | 7.180 |
| 2017 | 17.6661 | 2018 | - |
| 2018 | 24.7320 | 2019 | 3.540 |
| 2019 | 42.7407 | 2020 | 11.777 |
| 2020 |  | 2021 | 2.140 |



Figure 1: Plots of the data points in normal space for (a) 1985-2020, (b) 2005-2020 and (c) 2005-2020, but excluding 2010 . The 2021 survey result of 2.14 is indicated by the grey horizontal line.


Figure 2: Plots of the residuals of the fit of equation (1) against year for Analysis (II) and (a) 1985-2020, (b) 2005-2020 and (c) 2005-2020, but excluding 2010.


Figure 3: Further diagnostic plots related to the data used for the fits of equation (1), showing those for 1985 to 2020 on the left and for 2005 to 2020 on the right. Plot (ii) in terms of the logarithms of the ratios is added with a view to greater symmetry in a situation where the values in (i) are necessarily positive. The estimates of $k$ from equation (1) are indicated.


Figure 4: Probability density function plots for the log-normal distribution for the expected November recruitment given the regression results. The top plot (a) shows the predictions that would have been made in 2020 given the current recruitment series at that time (i.e. the current series truncated at 2019) along with the actual November 2020 recruitment estimate. The bottom plot (b) shows the distributions for the expected November 2021 recruitment estimate predicted from the regression given the 2021 survey result of 2.14. The 90\% Cls are also shown.


Figure 5: Plots of the November recruitment estimates against year, showing their mean and medians, for (I) the predictions that would have been made in 2020 based on the current recruitment series truncated at 2019 and (II) the current predictions for the 2020 November recruitment estimate based on the 2021 survey estimate. Results are shown for all data, and for 2005 onwards, to 2020. The means and medians on the left hand side plots (I) are to 2019, while for the right hand side plots (II) to 2020. Note that the November recruitment corresponds to the year prior to the corresponding value shown on the horizontal axis.


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